## Comparative study on non-linear and linear least square analyses applied to X-ray induced Auger electron spectroscopy transitions

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With the exception of the modified Auger parameter, X-ray induced Auger electron (X-AES) transitions aren't exploited to their full potential. Indeed, they can provide as much information (oxidation degree, chemical environment, atomic composition) as the classic photopeaks used in XPS, but their shapes' complexities limit their decompositions.

We offer here to explore the decomposition of Ga  $L_3M_{4,5}M_{4,5}$  and In  $M_{4,5}N_{4,5}N_{4,5}$  X-AES lines by comparing two approaches: the non-linear [1] and the linear [2] least square analyses. By combining non-linear and linear fitting procedures, PCA, and vectorial method [3], those

two analyses have been implemented on the materials  $Cu(In_xGa_{1-x})Se_2$  and InSb, to unveil their surface oxidation when exposed to different atmospheres. The growth of oxide phases (Ga<sub>2</sub>O<sub>3</sub> and In<sub>2</sub>O<sub>3</sub>, determined by PCA, vectorial method and by comparison with reference spectra) was monitored on the X-AES lines with non-linear linear and approaches, showing a very good



coherence between both, as illustrated

in Fig 1 for the In  $M_{4,5}N_{4,5}N_{4,5}$  X-AES transition of InSb. We will provide keys to perform non-linear and linear least squares analysis on X-AES lines, to explore new approaches for chemical determination.

[1] J.J. Moré, Numer. Anal. 630, 105 (1978).

<sup>[2]</sup>G.H. Golub and C. Reinsch, Linear Algebr. 420, 403 (1971).

<sup>[3]</sup> S. Béchu et al., Appl. Surf. Sci. 447, 528 (2018).

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## **Supplementary Pages (Optional)**

In Figure S1, we provide the example of Ga  $L_3M_{4,5}M_{4,5}$  non-linear and linear least square approaches for CIGS material after aging. When using the non-linear approach, 5 arbitrary photopeaks are necessary to simulate the CIGS environment and 5 others for the Ga<sub>2</sub>O<sub>3</sub> one. The fit results thus in a decomposition with 10 photopeaks while reference spectra of Ga in CIGS and in Ga<sub>2</sub>O<sub>3</sub> are injected within the linear least square decomposition. If the fit is easier to perform with the linear least square decomposition (less error), its quality is slightly improved when using the non-linear least square decomposition approach. This aspect will be also evocated.



Figure S2 Curves to fitted data of CIGS using nonlinear (left) and linear (right) approaches.

To show the coherence of the two approaches over a set of evolving data, we followed the percentage of  $Ga_2O_3$  growth in CIGS  $Ga L_3M_{4,5}M_{4,5}$  X-AES transition over time. Table S1 resumes this evolution for the non-linear and the linear approaches and the relative errors remain inferior to 5% for all the comparative data.

		t <sub>0</sub>	t <sub>1</sub>	t <sub>2</sub>	t <sub>3</sub>	$t_4$	t <sub>5</sub>	t <sub>6</sub>	t <sub>7</sub>	t <sub>8</sub>
Ga <sub>2</sub> O <sub>3</sub> at. %	Non-linear approach	0.1	27.9	35.2	39.6	42.9	41.3	45.4	46.3	53.4
	Linear approach	0.0	27.6	34.3	39.1	42.3	41.1	45.9	45.9	53.1
Relative error (%)		0.0	1.1	2.6	1.3	1.4	0.5	1.1	0.9	0.6